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Wroclaw University of Science and Technology, Chair of Electronics and Photonics Metrology, Boleslawa Prusa 53/55, 50-317 Wroclaw, Poland

ABSTRACT
In the atmosphere, black carbon aggregates interact with both organic and inorganic matter. In many studies they are modeled using different, less complex, geometries. However, some common simplification might lead to many inaccuracies in the following light scattering simulations. The goal of this study was to compare the spectral behavior of different, commonly used soot particle models. For light scattering simulations, in the visible spectrum, the ADDA algorithm was used. The results prove that the relative extinction error $\delta C_{ext}$, in some cases, can be unexpectedly large. Therefore, before starting excessive simulations, it is important to know what error might occur.

Keywords: Light scattering, Black carbon, Soot, Fractal-like aggregates, Discrete Dipole Approximation

1. INTRODUCTION
Small particles connect to each other and create geometries, namely aggregates, which can be described using the following fractal equation:\textsuperscript{1,2}

$$N_p = k_f \left( \frac{R_g}{r_p} \right)^{D_f}.$$ \hspace{1cm} (1)

in which $D_f$ and $k_f$ are the fractal dimension and the fractal prefactor respectively. $N_p$ is the number of monodisperse primary particles, $r_p$ is their radius and $R_g$ is the radius of gyration, which can be calculated using the formula:\textsuperscript{*}

$$R_g^2 = \frac{1}{N_p} \sum_{i=1}^{N_p} (\vec{r}_i - \vec{r}_0)^2 = \frac{1}{2N_p^2} \sum_{i,j} (\vec{r}_i - \vec{r}_j)^2,$$ \hspace{1cm} (2)

where $\vec{r}_i$ is the vector defining the location of the $i$–th primary particle and $\vec{r}_0$ is the mass center of the investigated geometry:

$$r_0 = \frac{1}{M} \sum_{i=1}^{N_p} \vec{r}_i m_i.$$ \hspace{1cm} (3)

In this equation, $M$ is the total mass of the aggregate and $m_i$ stands for the mass of the $i$–th primary particle. It is a reliable approximation for large, monodisperse aggregates (however, Eq. (1) might be also used when polydispersity is relatively low).

In this paper, soot particles were investigated. Commonly, they can be found in the troposphere.\textsuperscript{7} Their core element, namely the fractal-like aggregate of black carbon particles, is a product of incomplete combustion of carbon-based fuels.\textsuperscript{8} After generation, it interacts with both organic and inorganic matter and undergo morphological changes in the atmosphere.\textsuperscript{9} Here, to create soot particles three materials were used and their complex refractive indices $m$ are presented in Fig. 1. The first of them, namely for black carbon, was adapted from the paper by Chang et al.\textsuperscript{10} It is valid for particles generated in propane-oxygen flame. In their experiment, the equivalence ratio was 1.8 and the height above burner was determined as 10mm. Furthermore, the resulting $m_c$ in good agreement with the strict criterion proposed by Bond et al.\textsuperscript{8} Next, the refractive index for sulfate

email: krzysztof.skorupski@pwr.edu.pl

\textsuperscript{*}However, alternative equations can be also found in the literature.\textsuperscript{3–6}
(inorganic matter) was adapted from the OPAC database (the humidity was assumed to be 0%). Finally, the refractive index for organic acids (organic matter) was taken from the work by Myhre et al. The proportion of these three components is not fixed and changes along with the geographical location as well as the age of the soot particle. In many cases, the fraction of black carbon can be 7% (this value was used in the following part of the study) or even less.

There are many ways and methods to create fractal-like aggregate models. In this work the tunable CC algorithm by Filippov et al. was used. The modification by Skorupski et al. sped up the aggregation process and made the position error almost non-existent. The parameters for creating soot particles were based on various publications. Note, that many techniques for retrieving morphological parameters are known and each one might lead to slightly different results. Here, the reference black carbon aggregate model was composed of $N_{pc} = 20$ primary particles with the radius $r_p = 15\text{nm}$. For the first part of the study, primary particles were spherical and no polydispersity was implemented. To avoid positioning primary particles in point contact, small cylindrical necks, i.e. $Y_a = 0.15$, were added. The neck size parameter is defined as follows:

$$Y_a = \frac{r_c}{r_p},$$

where $Y_a$ is the dimensionless neck size parameter, $r_p$ stands for the radius of the smaller particle and $r_c$ is the radius of the minimum cross section of the investigated neck. The fractal dimension was $D_f = 2.2$ and the fractal prefactor was $k_f = 0.8$. The core fractal-like aggregate model is presented in Fig. 2A.

Light scattering techniques have been commonly used to measure and investigate different objects, like: erythrocytes, fibres, fractal-like aggregates, and much more. The absorption properties of black carbon can not be neglected. It is considered as one of the most influential material when the global warming effect is studied. Here, to measure its optical properties the ADDA algorithm was used. It is based on the DDA (Discrete Dipole Approximation) method which gives accurate results when the investigated geometry is composed of a sufficient number of volume elements (dipoles). However, it is less accurate when the material is highly absorbent, like black carbon. For this reason, every primary particle was decomposed into at least $N_d \approx 1000$ volume elements (dipoles). The distance between them in the resulting mesh was $d = 2.4\text{nm}$. The polarizability expression was IGT:SO (approximate Integration of Green’s Tensor over the dipole). It was proved that it is reliable in the investigated case. Other ADDA parameters were set to their default values. To obtain the most accurate data, all results were orientationally averaged using the Romberg integration technique (the maximum number of orientations was 256). A detailed study concerning the use of the DDA method with black carbon particles can be found in the previous work by Skorupski. In the same paper, a comparison between

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†The algorithm is a part of the FLAGE (Fractal-Like Aggregate Generation Environment) software which can be downloaded from: http://scattering.eu/.

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Figure 1. Complex refractive indices $m$ used in the study, namely: black carbon $m_c$, sulfate $m_s$, organic acid $m_a$. **Figure 1. Complex refractive indices $m$ used in the study, namely: black carbon $m_c$, sulfate $m_s$, organic acid $m_a$.**
two scattering methods, namely ADDA and T-Matrix, was performed.\textsuperscript{57–60} Here, the incident wavelength varied from $\lambda = 400\text{nm}$ to $\lambda = 800\text{nm}$ with the step $\Delta\lambda = 50\text{nm}$.

2. LIGHT SCATTERING SIMULATIONS

Soot particle models are usually simplified (e.g. to speed up the following light scattering simulations). However, it leads to inaccuracies and simulation errors. In this sections, a few common cases are described.

The most radical simplification is to use, instead of a proper fractal-like aggregate model, a sphere of equivalent volume (Fig. 2B). However, when the extinction cross section $C_{\text{ext}}$ is investigated, the changes might not be so extreme, what is presented in Fig. 3. Note, that the results are valid for black carbon aggregates and they prove, that the studied parameter is mostly dependent on the volume.

Next, five sulfate particles were added to the core geometry (Fig. 4A). Their radius was $r_p = 15\text{nm}$. In the next model the five spherical particles were replaced with two ellipsoidal particles (Fig. 4B). However, the sulfate volume remained constant. This is a slightly more realistic approach. The difference in $C_{\text{ext}}$ is presented in Fig. 5. It proves that, even when the volume is conserved, the size, shape and location of elements can alter the resulting diagrams. In this case by ca. $\delta C_{\text{ext}} \approx 3\%$. Additionally, two more geometries were investigated. The first one was a sphere with an external sulfate layer with the thickness $t_s \approx 3.144\text{nm}$ (Fig. 4C). The last
one, used in this part of study, was an equivalent volume sphere, decomposed into a mesh of volume elements (dipoles). There was no strict division between black carbon and sulfate because the location of volume elements (dipoles) was randomized. The total volume of the two materials was always the same. The light scattering simulation results, presented in Fig. 5, were compared to those for the fractal-like aggregate model enriched with two non-spherical particles. Once again, the results prove that the position of elements has an impact on the extinction diagrams and should be taken into consideration before creating realistic soot models.

![Figure 4](https://example.com/fig4.png)

**Figure 4.** The geometries used for the light scattering simulations: A) The core black carbon aggregate with five spherical sulfate particles. B) The core black carbon aggregate with two ellipsoidal sulfate particles. C) The sphere of equivalent volume.

![Figure 5](https://example.com/fig5.png)

**Figure 5.** Left) The relative extinction error \( \delta C_{\text{ext}} \) between geometries presented in Fig. 4A and Fig. 4B (reference). Right) The relative extinction error \( \delta C_{\text{ext}} \) for the two spherical models (covered by the external layers and composed of mixed materials).

In the next study, inorganic matter, i.e. organic acid, was added. Fig. 6A presents the investigated aggregate model composed of \( N_{pc} = 15 \) black carbon, \( N_{ps} = 5 \) sulfate, and \( N_{pa} = 15 \) organic primary particles. All of them were characterized by the radius of \( r_p = 15nm \). The light scattering simulations (Fig. 7) were compared to those, obtained by calculating the spectral behavior of a slightly more complex geometry. The more advanced model (Fig. 6B) was composed of \( N_{pc} = 15 \) spherical black carbon particles, \( N_{ps} = 2 \) ellipsoidal sulfate particles and an external organic layer with the thickness \( t_a = 2.000nm \) (the total volume of the three materials was conserved). This time, by adding organic particles, the geometry was artificially extended what resulted in much more visible discrepancy in \( C_{\text{ext}} \). The results prove that external layers should not be modeled as additional particles. Similarly to the previous step, two more spherical geometries were generated. The first one (Fig. 6C) was covered by two layers. The first one was inorganic (sulfate, \( t_s \approx 3.144nm \)) and the second one was organic.
Finally, the most advanced soot particle was generated. The normal distribution used for its generation was as follows: the mean particle radius $\bar{r}_{pc} = 15\text{nm}$, the standard deviation of the particle radius $\sigma r_{pc} = 1\text{nm}$, the mean neck size $Y_a = 0.5$, the standard deviation of the neck size $\sigma Y_a = 0.1$. Again, the fractal dimension was $D_f = 2.2$ and the fractal prefactor was $k_f = 0.8$. Next, two sulfate particles, like in the previous study, were added. All particles were replaced with their equivalent volume ellipsoidal representations. Finally, an external organic layer was added. This time it was much thicker because the volume fraction of black carbon was estimated as $7\%$. The soot particle model is presented in Fig. 8A. Because the diameter of the resulting geometry was much larger, the distance between volume elements (dipoles) was increased to $d = 3\text{nm}$. All the other parameters were the same. The extinction cross section $C_{ext}$ for the whole particle, as well as for its materials, can be found in Fig. 9. As before, two spherical geometries, characterized by the same volume, were generated. The first one, which is the black carbon sphere covered by two additional layers, is presented in Fig. 8B. The second one is an assembly of mixed volume elements (dipoles). This time the results prove that the randomly positioned volume elements (dipoles) lead to much worse results than external, spherical layers.
Figure 8. The geometries used for the light scattering simulations: A) The soot particle composed of three materials, namely black carbon, sulfate, organic acid. B) The sphere of equivalent volume.

Figure 9. Left) The extinction cross section $C_{ext}$ for the geometry presented in Fig. 6A. Right) The impact of the three materials on the resulting extinction cross section $C_{ext}$.

Figure 10. The relative extinction cross section error $\delta C_{ext}$ for the two spherical models (covered by the external layers and composed of mixed materials). The reference was the geometry presented in Fig. 8A.
3. CONCLUSIONS

In the study three different soot particle models were investigated. The results prove that the position, size and shape of particles has an undeniable impact on the extinction cross section $C_{ext}$, even when the total volume of used materials remains the same. To improve the quality of simulations of the light scattering process a proper aggregate models must be used.

4. ACKNOWLEDGEMENT

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